Solving Exponential Equations (Part 1)

These notes are intended as a summary of section 5.3 (p. 358 - 363) in your workbook. You should also read the section for more complete explanations and additional examples.

Laws of Exponents

- $1. \quad x^m \cdot x^n = x^{m+n}$
- $2. \quad (x \cdot y)^m = x^m \cdot y^m$
- $3. \quad \frac{x^m}{x^n} = x^{m-n}$
- $4. \quad \left(\frac{x}{y}\right)^m = \frac{x^m}{y^m}$
- $5. \quad \left(x^m\right)^n = x^{m \cdot n}$
- $6. \quad \sqrt[m]{x} = x^{\frac{1}{m}}$

$$7. \quad x^{-m} = \frac{1}{x^m}$$

Exponential Equations

An **exponential equation** is an equation that contains a power with a variable in the exponent. For example:

$$3^x = 81$$

Equations of this type can be solved by writing both sides as powers with the same base, as shown below:

$$3^x = 3^4$$

Logically, if the powers are equal, and their bases are equal, then their exponents must also be equal. Thus,

x = 4

Example 1 (sidebar p. 359) Solve each equation.

a)
$$4^x = \frac{1}{256}$$

b) $27^x = 9^{2x-1}$

Example (not in workbook) Solve each equation.

a)
$$2^x = 8$$

b)
$$3^x = \frac{1}{27}$$

c)
$$2^{-x} = \frac{1}{32}$$

d) $5^{x^2-2x} = 125$

e) $81^{x+2} = 27^2$

f) $2 \cdot 4^{x-3} = 32$

Example 2 (sidebar p. 360) Solve each equation.

b) $\left(\sqrt{125}\right)^{2x+1} = \sqrt[3]{625}$

a)
$$2^x = 8\sqrt[3]{2}$$

Homework: #3 – 6, 9, 10 in the exercises (p. 364 – 368). Answers on p. 369.